Featherstone Primary School Calculation Policy February 2018

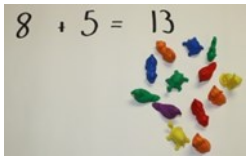
Aspire, Believe, Succeed

Year 1 Calculation

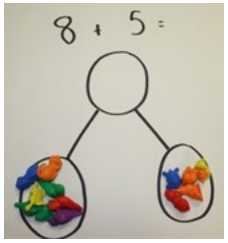
Addition : Add one-digit and two-digit numbers to 20 including 0.

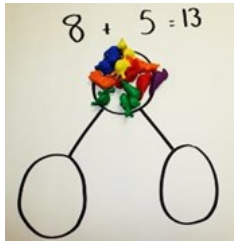
In Year 1, children become familiar with numbers 1-20 before learning how to add. All children begin using concrete objects to conceptually understand the process of addition in a variety of representations. Children then move on to using pictorial versions of these representations.

Concrete

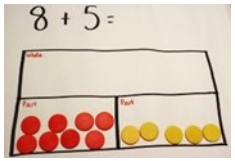


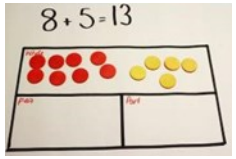
Children count physical objects. Counting one group of 8, one group of 5 and combining these two groups to make 13.





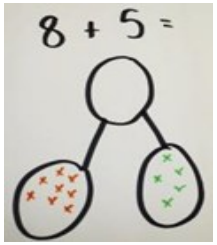
Children use physical objects to add using the circle part whole model.

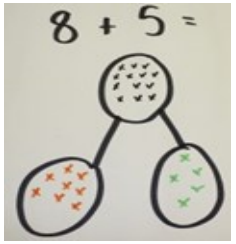




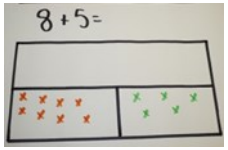
Children use physical objects to add using the bar model.

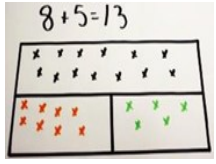
Pictorial





Progressing from the concrete method, children represent each physical object with crosses/ circles. Counting them altogether to find the total.





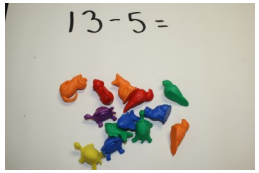
Progressing from the concrete method, children represent each physical object with crosses/ circles. Counting them altogether to find the total.

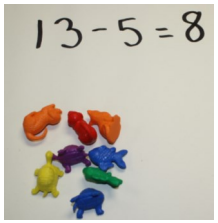
Year 1 Calculation

Subtraction: Subtract one-digit and two-digit numbers to 20 including 0.

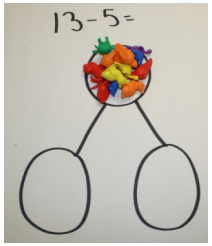
In Year 1, children become familiar with numbers 1-20 before learning how to subtract. All children begin using concrete objects to conceptually understand the process of subtraction in a variety of representations. Children then move on to using pictorial versions of these representations.

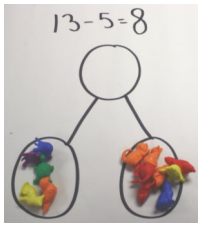
Concrete



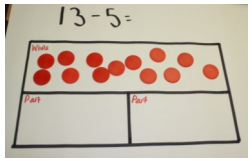


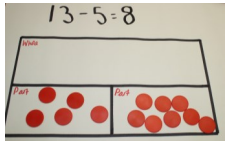
Children subtract by using physical objects. They count a group of 13 then take a group a 5 away and count how many are left.





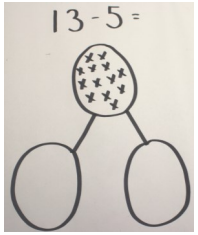
Children use physical objects to subtract using the circle part whole model.

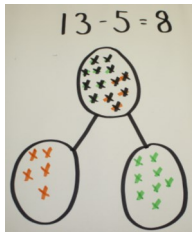




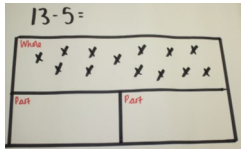
Children use physical objects to subtract using the bar model.

Pictorial





Progressing from the concrete method. Children represent each physical object with crosses/ circles.



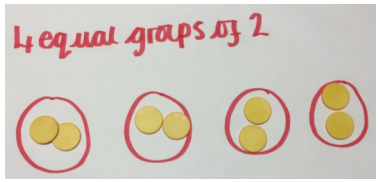
Progressing from the concrete method, children represent each physical object with crosses/ circles using the bar model.

Year 1 Calculation

Multiplication: Solve one-step problems involving multiplication.

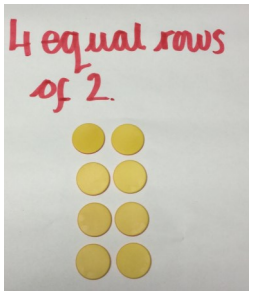
In Year 1, children become familiar with both concrete and pictorial methods of multiplication. Children understand multiplication as making equal groups.

Concrete



Children use concrete objects to multiply whether this be using counters or counting objects. They understand multiplying as making equal groups.

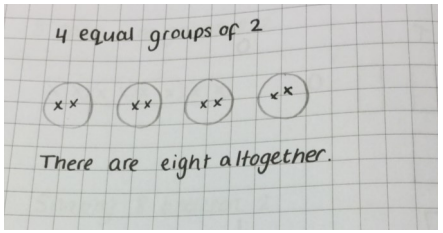
They draw 4 equal groups and put two in each group. There are 8 in total.



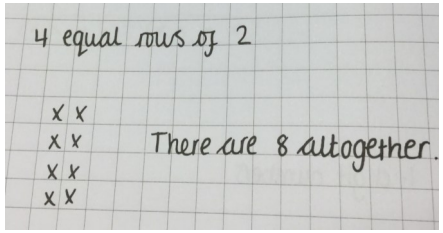
Children, with support, represent multiplication using arrays.

They understand this as 4 equal rows of 2 and count the total.

Pictorial



Children move onto a pictorial representation of the concrete method. They draw 4 equal groups and put two in each group. They then count how many there are in total.



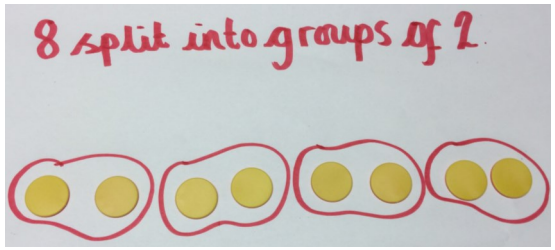
Children, with support, represent a concrete array using a pictorial method.

Year 1 Calculation

Division: Solve one-step problems involving division

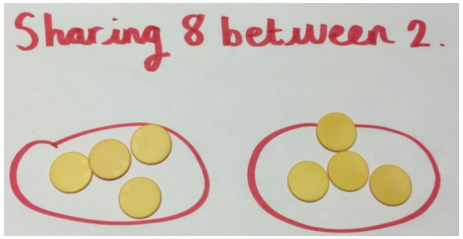
In Year 1, children become familiar with both concrete and pictorial methods of division. They understand the difference between making groups and sharing.

Concrete



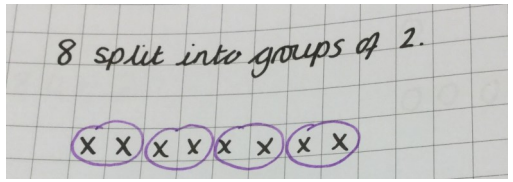
Children use counters or counting objects to answer divisions.

They begin by getting the correct number of counters , in this case 8. Then split these into groups of 2.

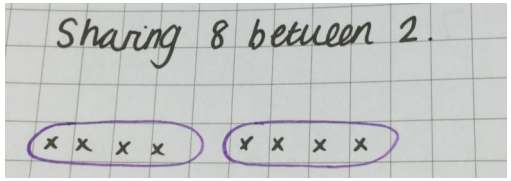


When sharing, children begin by getting the correct number of counters. They then share these between the number of groups. In this case, 8 shared between 2 groups.

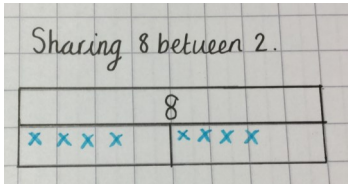
Pictorial



Moving on from the concrete method, children draw crosses rather than use counters then group these into the correct amount. In this case, groups of 2.



When sharing children draw the number of circles then share the amount between these circles.



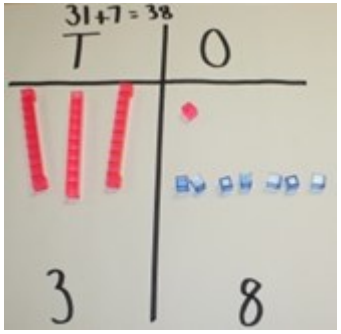
Children move on to represent the division using a bar model.

Year 2 Calculation

Addition: Add a two-digit number and a one-digit number.

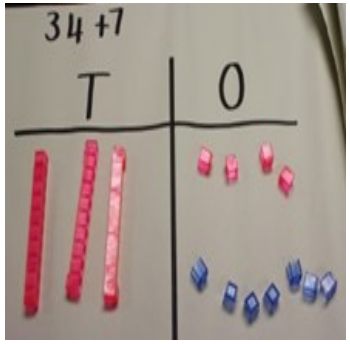
In year 2, children progress to a more formal concrete method of addition using a place value chart. Base ten supports the transition from a concrete method to a pictorial method of addition as well as addition crossing the tens boundary.

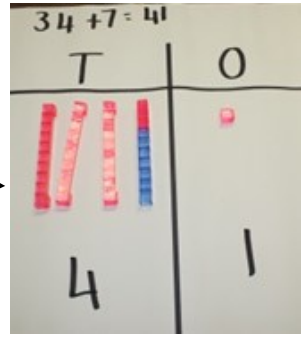
Concrete



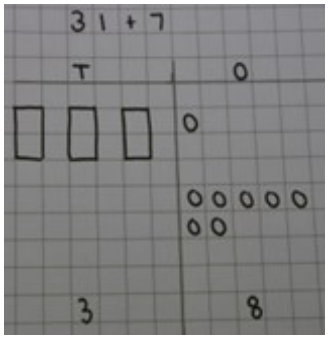
Children begin by addition one digit numbers where the answer does not cross the tens boundary. In the example to the left, 31 Is represented in pink and 8 in blue. Children count the number of units and the number to tens to find the answer. Beginning in the units column.

Children progress into adding where the calculation crosses the tense boundary. In the example below children can use ten ones to make a new tower of ten.





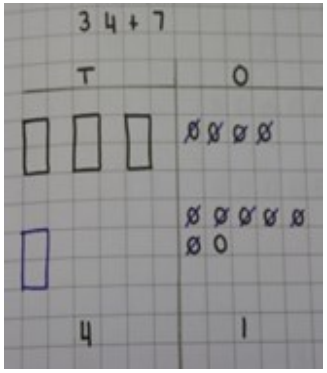
Pictorial



When moving to pictorial methods, children use a written variation of the base ten used previously.

Each number is drawn into the place value chart.

Children begin by adding the units and then the tens.



Children progress into crossing the tens boundary.

In the example to the left, both values have been drawn . It is recognised that there are more than ten units in the ones column and so these are crossed out (as seen in purple) and a new tower of ten is drawn.

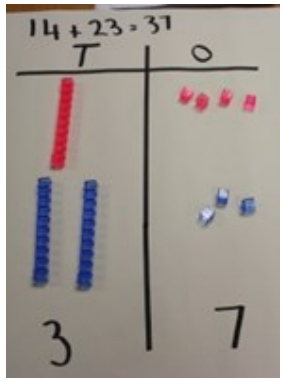
Children then count the remaining units first and then the tens.

Year 2 Calculation

Addition: Add two two-digit numbers.

In year 2, children progress to a more formal concrete method of addition using a place value chart. Base ten supports the transition from a concrete method to a pictorial method of addition.

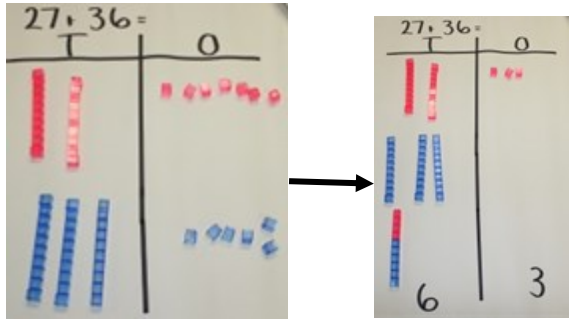
Concrete



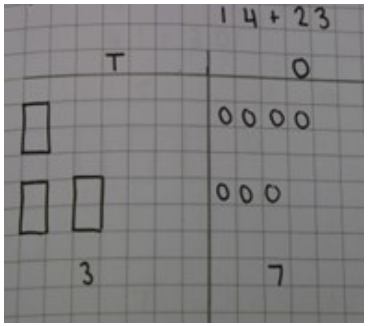
Children begin by adding two two-digit numbers that do not cross the tens boundary. In the example to the left ,14 is represented in pink and 23 is represented in blue . The number of units are counted followed by the number of tens in order to calculate the total.

Children progress into adding two-digit numbers where the answer crosses the tens boundary. The two numbers are represented in pink and blue. It has been recognised that there are more than ten ones and so a new tower of ten can be made.

The remaining ones and the tens are counted to calculate a total.

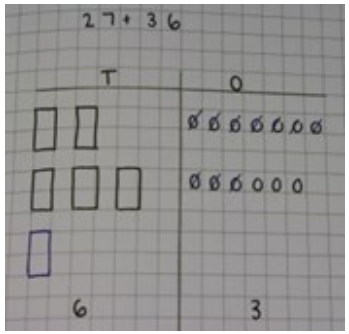


Pictorial



When moving into a pictorial method, children use a written variation of base ten. Children draw both numbers into the place value chart.

They begin by adding the units and then adding the tens to find a total.



Children progress into a pictorial method of adding two-digit numbers where the answer crosses the tens boundary. The two numbers are drawn into the place value grid. It has been recognised that there are more than ten ones so 10 of these have been crossed out (in purple) and a new tower of ten has been drawn.

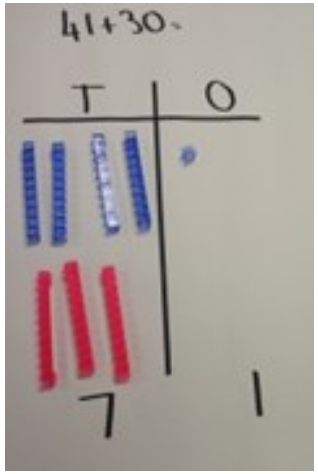
The remaining ones and the tens are counted to calculate a total.

Year 2 Calculation

Addition: Add a two-digit number and a multiple of ten.

In year 2, children learn concrete and pictorial methods of adding a two-digit number and a multiple of ten. Children may progress and talk about how this calculation may be done mentally.

Concrete

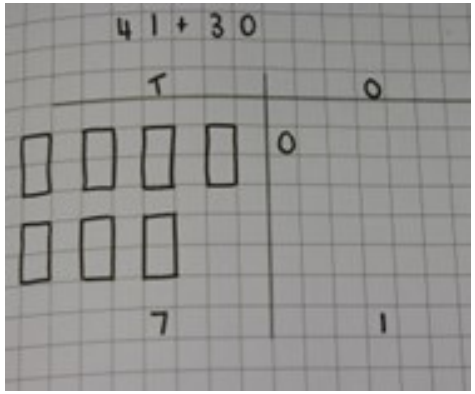


Children and shown how to complete this calculation using base ten equipment.

41 and 30 are represented with the blue and pink base ten.

Children count the ones and the tens column to find a total.

Pictorial



Children progress into using a pictorial representation of base ten.

They draw each value into their place value grid and then add the tens and the units.

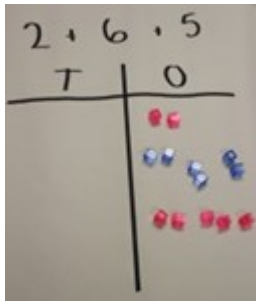
Year 2 Calculation

Addition:

Add three one-digit numbers

In Year 2, children learn to add three one-digit numbers. Children should learn that they can add the three numbers in any order due to the commutative nature of addition.

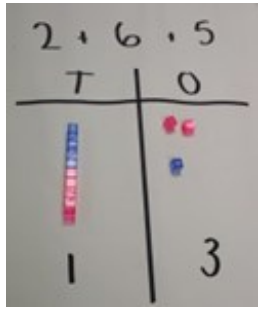
Concrete



Children and shown how to complete this calculation using base ten equipment.

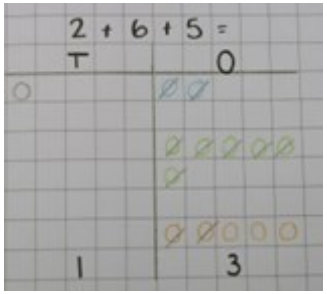
2,6 and 5 are all drawn into the ones column of the place value grid.

It is recognised that there are more than ten ones so these are grouping together to make a tower of ten.



Children count the remaining ones and the number of tens that they have.

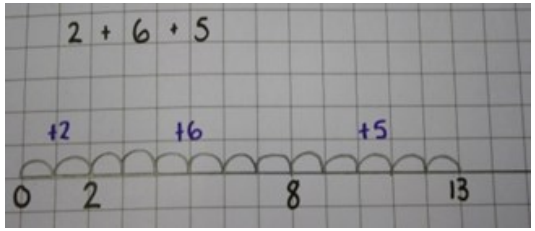
Pictorial



Children progress into using a pictorial version of base ten.

Each of the one-digit numbers are represented in a different colour.

It is recognised that there are more than ten ones and so these are crossed out to make a tower of ten.



As an alternative method, children may use a number line to add the three numbers.

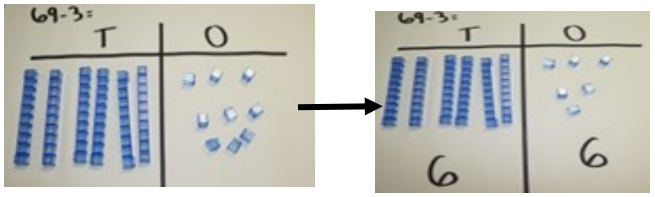
Starting at zero then making the correct amount of jumps.

Year 2 Calculation

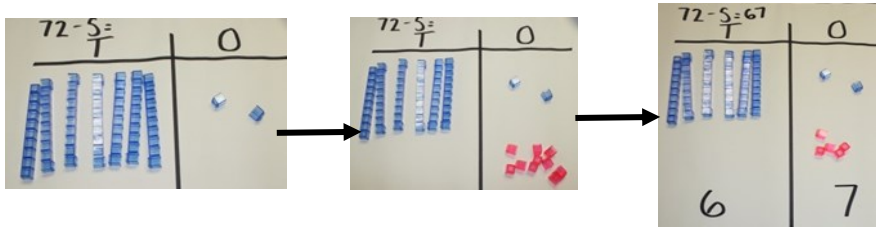
Subtraction: Subtract a two-digit number and a one-digit number.

In year 2, children progress to a more formal concrete method of subtraction using a place value chart. Base ten supports the transition from a concrete method to a pictorial method of subtraction as well as subtraction crossing the tens boundary.

Concrete



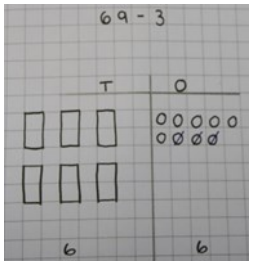
Children begin by using base ten to subtract a one-digit number from a two-digit number which does not require exchange. In the above diagram, children represent the starting value in the grid. They take the required number of ones and write the value that remains.



Children progress into exchange. They represent the starting value in the grid. It is recognised that there are only 2 ones and so we can not take the required 5 away.

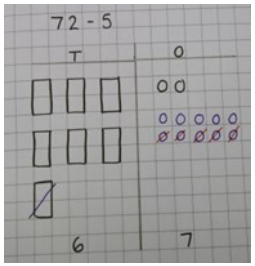
As seen in pink, one ten is exchanged for ten ones. The 5 ones can then be subtracted. The remaining ones and tens are counted to complete the answer.

Pictorial



Children progress into a pictorial version of using base ten.

Children draw the starting number into their place value grid. They cross out the required number of ones and write the amount that remains.



When exchange is required, children begin using the same process. They represent the starting number in their place value grid.

It is recognised that there are not enough ones to take away.

Children cross out one tower of ten and exchange this for ten ones (as seen in purple on the example).

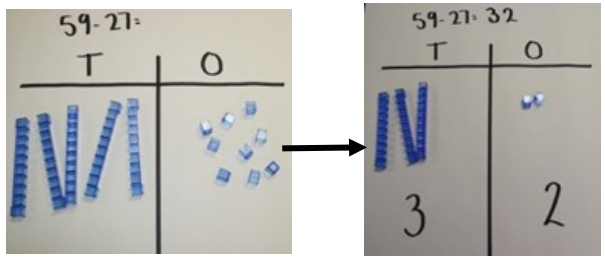
The required 5 can then be subtracted.

Year 2 Calculation

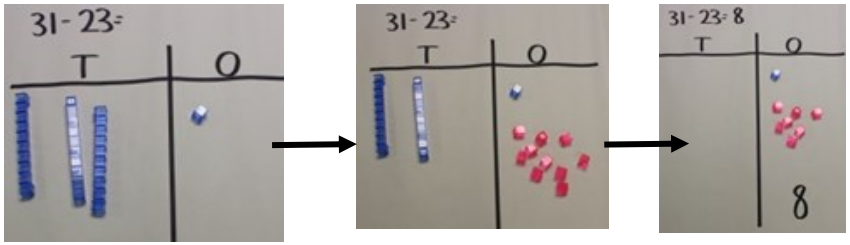
Subtraction: Subtract two two-digit numbers.

In year 2, children progress to a more formal concrete method of subtraction using a place value chart. Base ten supports the transition from a concrete method to a pictorial method of subtraction as well as subtraction crossing the tens boundary.

Concrete

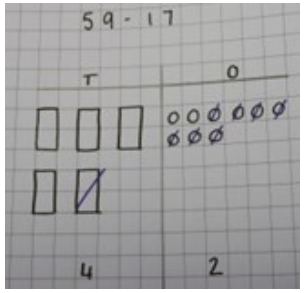


Children begin by using base ten to subtract a two-digit number from a two-digit number which does not require exchange. In the above diagram children represent the starting value in the grid. They take the required number of ones away followed by the required number of tens to find the correct answer.



Children progress into questions where they need to exchange. In the above diagram, children represent the starting value in the grid. It is recognised that they can not take away the required number of ones and therefore need to exchange a tower of ten (as seen in pink). They can then take the required number of ones followed by the required number of tens to find the correct answer.

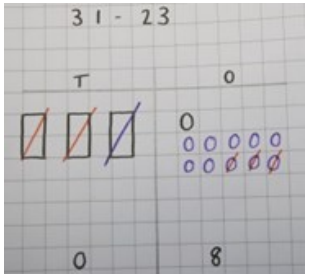
Pictorial



Children move into a pictorial method of subtraction.

They draw the starting value into the grid.

They subtract the required number of ones and the required number of tens (as seen in purple). Then count the remaining ones and tens to find the answer.



Children move into a pictorial method where they need to exchange.

They draw the starting value into the grid.

They recognise that they can not subtract the required number of ones and so exchange a tower of ten (as seen in purple) they can then subtract the correct number of ones and then tens (as seen in orange).

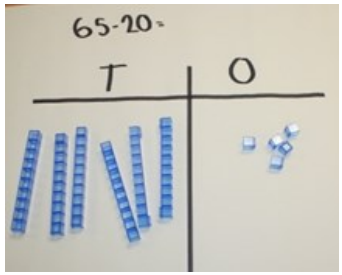
Finally, they count the remainder to complete the answer.

Year 2 Calculation

Subtraction: Subtract a two-digit number and a multiple of ten.

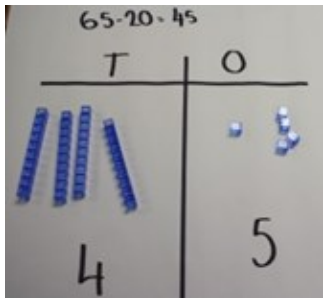
In year 2, children learn concrete and pictorial methods of subtracting a two-digit number and a multiple of ten. Children may progress and talk about how this calculation may be done mentally.

Concrete

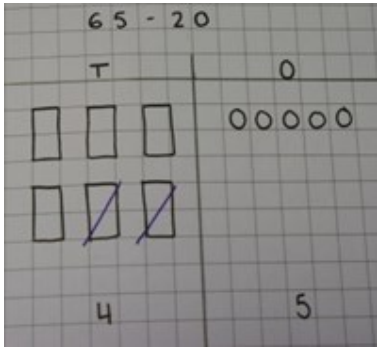


Children begin by using base ten to subtract a two-digit number and a multiple of ten.

Children begin by representing the starting value using base ten then taking away the required number of tens.



Pictorial



Children progress into a pictorial method of base ten.

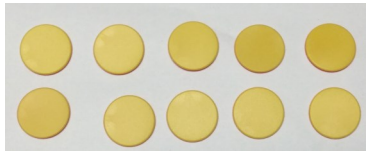
They draw the starting value into the grid then cross the required number of tens to find the correct answer.

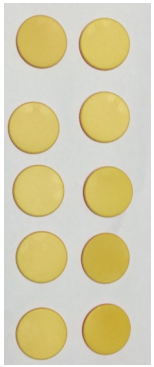
Year 2 Calculation

Multiplication: Calculate mathematical statements for multiplication within the multiplication tables using the multiplication symbol (x) and equals symbol (=).

In year 2, children use concrete representations to support a range of pictorial methods to multiply. Children understand the commutative nature of multiplication and that their array will look different dependant upon the order of numbers within the multiplication.

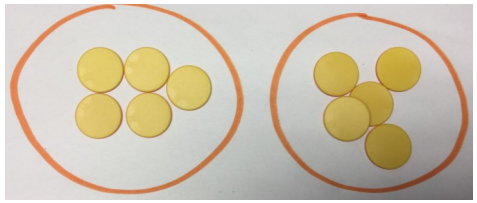
Concrete



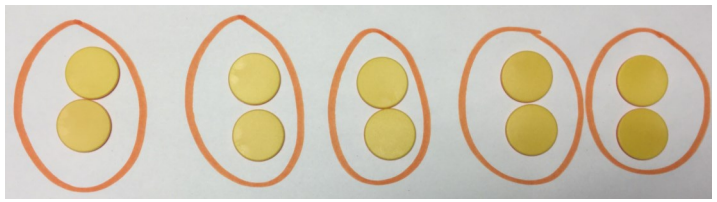


Children can use counters, or other objects, to represent arrays.

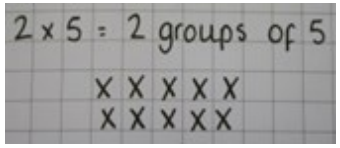
These are labelled correctly. In the first example 2 groups of 5 (2x 5) and in the second example 5 groups of 2 (5x2).

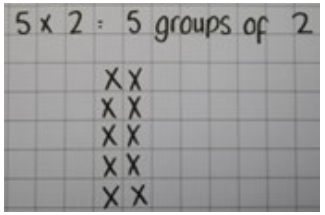


Children use concrete objects to multiply making equal groups.

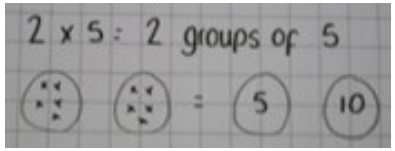


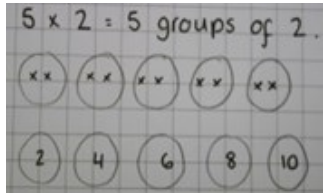
Pictorial





Children can draw an array to solve a multiplication with the number of groups going horizontally down and the amount within the group going vertically across as seen above.





Children can draw circles to show the number of groups and place dots/ crosses within the circle to represent the amount within that group.

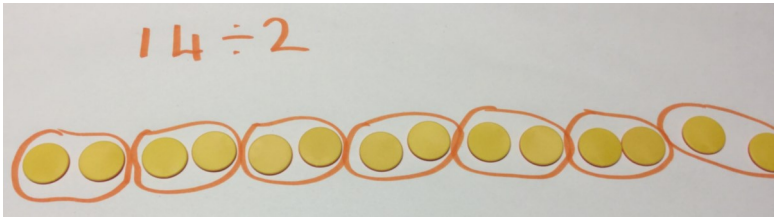
They can then progress to writing the number in that group in digit form showing a running total .

Year 2 Calculation

Division: Calculate mathematical statements for division with the multiplication tables using the division symbol (÷) and equals symbol (=).

In Year 2, following on from initial understanding in Year 1 children understand the difference between sharing and grouping.

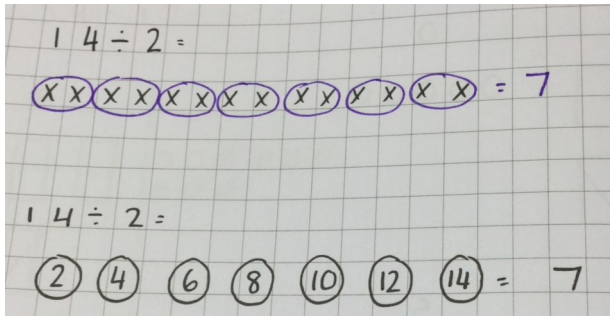
Concrete



Children can use concrete objects to divide whether this be counters or counting objects.

Children get the correct number of counters and share these into groups of 2 giving 7 groups.

Pictorial



Children move onto pictorial method.

They draw the correct number of circles and the circle groups of 2 which gives 7 groups.

They develop this pictorial method further by drawing groups and writing 2 in each group to reach 14.

Year 3 Calculation

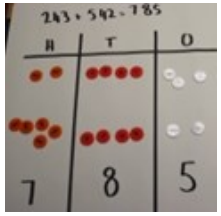
Addition: Use the formal written method of addition to add numbers with up to three digits.

In Year 3, children make the transition to formal written methods of calculation. Children need to have secure conceptual understanding of concrete and pictorial methods in order to do this.

NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

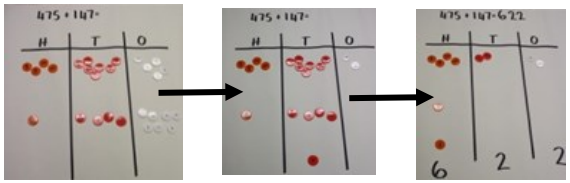
Concrete

Prior to using place value counters, children may use base ten (see addition in Year 2) to help support their understanding.



Children begin addition by calculating examples that do not require them to cross the tens boundary.

Each number is represented in the place value grid before children find the total starting in the ones col-

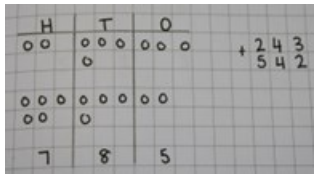


Children progress to questions which require regrouping. It is recognised that there are more than ten ones therefore children group together ten and regroup them to make one ten in the tens column. It is then recognised that there are more than 10 tens which are regrouped to make a hundred.

Children then count what remains to find their answer.

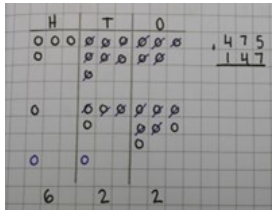
Note: when teaching this method progress carefully through the level of regrouping required.

Pictorial



Children begin addition by calculating examples that do not require them to cross the tens boundary.

Each number is represented in the grid before children find the total starting in the ones column.

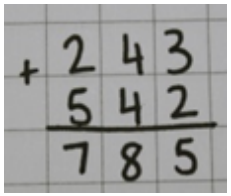


Children progress to questions which require regrouping. It is recognised that there are more than ten ones therefore children group together ten and regroup them to make one ten in the tens column. It is then recognised that there are more than 10 tens which are regrouped to make a hundred. This can be seen with the purple jottings.

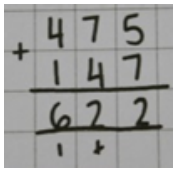
Children then count what remains to find their answer.

Note: when teaching this method progress carefully through the level of regrouping required.

Abstract



Children finally progress onto a formal written method of addition beginning with examples that do not require them to cross the tens boundary. The pictorial representation and the abstract representation are modelled alongside each other to develop conceptual understanding. Examples are taught where children need to use their place value knowledge to line up digits correctly.



Children progress to questions which require regrouping. It is recognised that there are more than ten ones therefore children group together ten and regroup them to make one ten in the tens column (as seen at the bottom). It is then recognised that seven tens and four tens make eleven tens altogether leaving one ten in the tens column and regrouping the ten tens into the hundreds column This can be seen in the jottings above.

Note: when teaching this method progress carefully through the level of regrouping required.

Year 3 Calculation

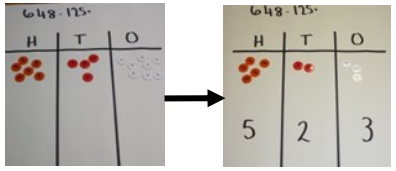
Subtraction: Use the formal written method of subtraction to subtract numbers with up to three digits.

In Year 3, children make the transition to formal written methods of calculation. Children need to have secure conceptual understanding of concrete and pictorial methods in order to do this.

NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

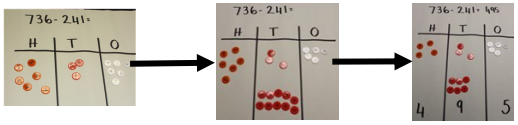
Concrete

Prior to using place value counters, children may use base ten (see subtraction in Year 2) to help support their understanding.



Children begin subtraction by calculating examples that do not require them to exchange.

Each number is represented in the place value grid before children find the answer starting in the ones column.

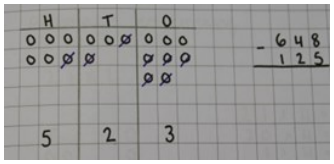


Children progress to questions which require exchange. It is recognised that they are able to subtract one from the ones column but unable to subtract 4 tens from the tens column. One hundred has been exchanged for ten tens which has allowed for the subtraction of the four needed. Two hundreds are then subtracted.

Children then count what remains to find their answer.

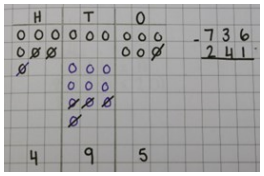
Note: when teaching this method progress carefully through the level of exchange required.

Pictorial



Children begin subtraction by calculating examples that do not require them to exchange.

Each number is represented in the place value grid before children find the answer starting in the ones column.

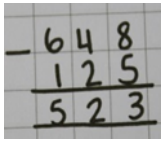


Children progress to questions which require exchange. It is recognised that they are able to subtract one from the ones column but unable to subtract 4 tens from the tens column. One hundred has been exchanged for ten tens which has allowed for the subtraction of the four needed. Two hundreds are then subtracted. This can be seen in the crossings out above.

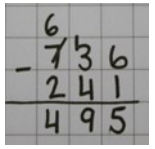
Children then count what remains to find their answer.

Note: when teaching this method progress carefully through the level of exchange required.

Abstract



Children finally progress onto a formal written method of subtraction beginning with examples that do not require them to exchange. The pictorial representation and the abstract representation are modelled alongside each other to develop conceptual understanding. Examples are taught where children need to use their place value knowledge to line up digits correctly.



Children progress to questions which require exchange. It is recognised that one unit can be subtracting from six units to leave five. Four hundreds can not be taken from three hundreds and so one hundred is exchanged for ten tens which can be seen in the jottings above. Children may then do six hundreds take away two hundreds leaving four. This can be seen in the jottings above.

Note: when teaching this method progress carefully through the level of regrouping required.

Year 3 Calculation

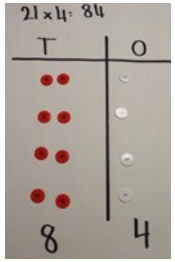
Multiplication: Write mathematical statements using multiplication facts they know including multiplying a two-digit number by a one-digit number.

In Year 3, children make the transition to formal written methods of calculation. Children need to have secure conceptual understanding of concrete and pictorial methods in order to do this.

NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

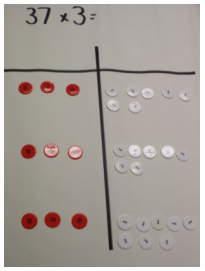
Concrete

Children may begin by using base ten to develop conceptual understanding before moving on to use place value counters.



Children make the number of groups in their place value grid . In this case, 4 groups of 21.

Similar to addition they add the ones and the tens to find the total.

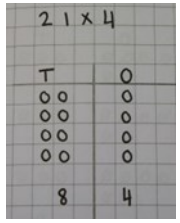


Children move onto multiplication which requires them to regroup.

Children make three groups of 37 in their place value grid.

They use their addition skills to find the total.

Pictorial



Children move on to a pictorial representation of the concrete method.

As seen in the example, children make the number of groups in their place value grid .

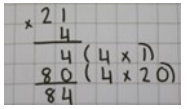
Similar to addition they add the ones and the tens to find the total.

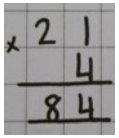
Children move onto multiplication which requires them to regroup.

Children make three groups of 37 in their place value grid.

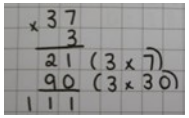
They use their addition skills to find the total.

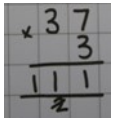
Abstract





To support progression into a formal written method, children first use an expanded written method. This is modelled alongside the pictorial method to support conceptual understanding. Once children are secure, they move onto the formal written method on the right.





To support progression into a formal written method, children first use an expanded written method. This is modelled alongside the pictorial method to support conceptual understanding. Once children are secure, they move onto the formal written method on the right. Children will need to recognise that 3 x 7 = 21 which is two tens and one unit and therefore carry the two tens across.

Year 3 Calculation

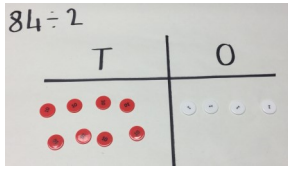
Division: dividing a two-digit number by a one-digit number progressing into formal written methods.

In Year 3, children make the transition to formal written methods of calculation. Children need to have secure conceptual understanding of concrete and pictorial methods in order to do this.

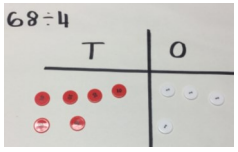
NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

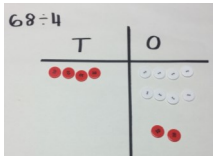
Concrete

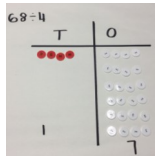
Children may begin by using base ten to develop conceptual understanding before moving on to use place value counters.



Children make the correct number In the place value grid. They group the 8 tens into groups of 2 and the 4 ones into groups of 2. There are 4 groups of tens and 2 groups of ones.

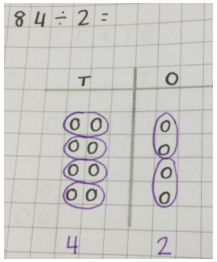






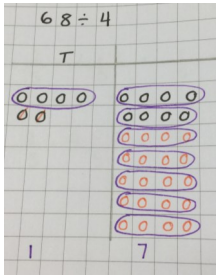
Children move onto examples where they need to regroup. Children make the correct number In the place value grid. They group the 6 tens into groups of 4. They can only make one group of 4 with two left over. They exchange these two tens into the ones column. They group to 28 ones into groups of 4 giving 7 groups.

Pictorial



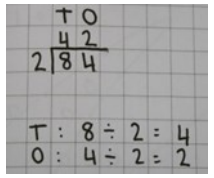
Children move onto a pictorial method.

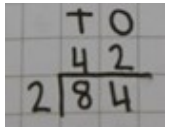
Children move onto a pictorial method. They draw 82 into their place value grid. They group the 8 tens into groups of 2 giving 4 groups and the 4 ones into groups of 2 giving 2 groups.



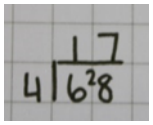
Children move onto examples where they need to regroup. They draw 68 into their place value grid. They group 6 tens into groups of 4. There is 1 group with 2 tens left over which they exchange into the ones column (as seen in orange). The 28 ones are then grouped into groups of 4 giving 7 groups.

Abstract





Children move onto an abstract method, initially making informal jottings to support as seen in the examples on the left.

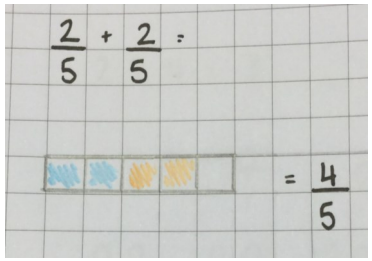


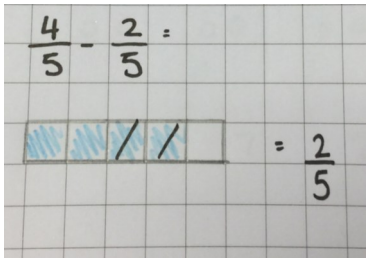
Year 3 Calculation

Fractions: Add and subtract fractions with the same denominator within a whole.

In Year 3 children begin to look at the addition of fractions through pictorial methods established in other fraction areas of learning.

Pictorial



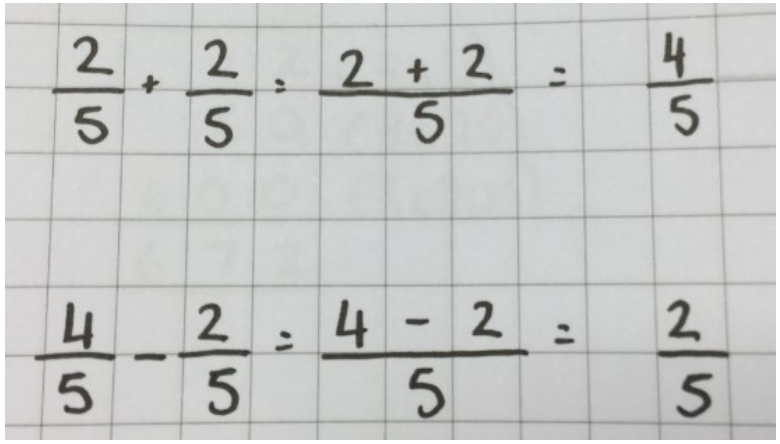


Children begin adding and subtracting fractions with the same denominator using fraction bars.

As seen in the first example children draw 2/7s. They then shade in 3 more— to give a total of 5/7..

When subtracting ,children begin by shading the correct amount. They then cross out the required number and count the remainder.

Abstract



Once secure, children move onto using a more abstract method.

Children recognise that when adding and subtracting fractions with the same denominator the denominator stays the same (as the sizes of the pieces are the same) we can then add or subtract the numerators.

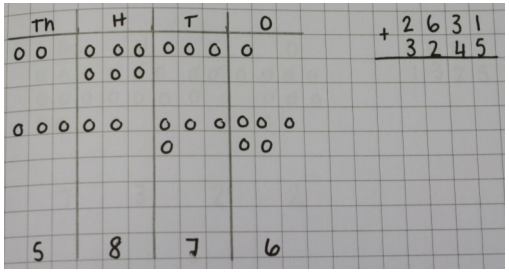
Year 4 Calculation

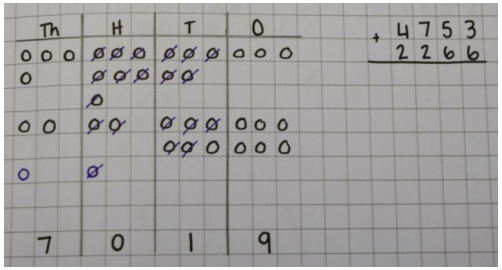
Addition: **Add four numbers up to four digits using the formal written method.**

In Year 4, children build upon calculation skills developed in Year 3. Prior to the methods taught below, concrete methods (as modelled in Year 3 addition) are used to support conceptual understanding.

NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

Pictorial



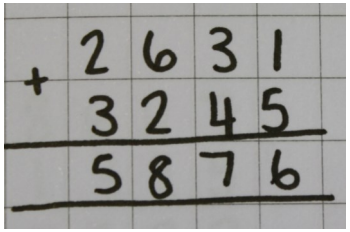


Children use a pictorial method to aid conceptual understanding of addition of whole numbers up to four digits. This includes adding numbers with different amounts of digits.

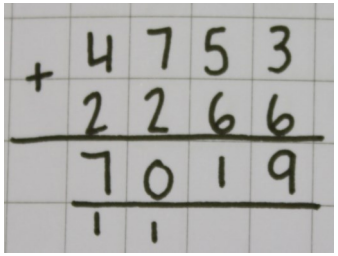
Examples are carefully structured to begin with those that do not require exchange.

When modelling this method, children's place value knowledge is reinforced. Looking at the second example. 3 ones add 6 ones is 9 ones. 5 tens add 6 tens is 11 tens which makes 1 hundred and 1 ten. We carry this 1 hundred into the hundreds column. 7 hundreds plus 2 hundreds plus 0 hundreds is 10 hundreds which makes 1 thousand which I carry into the thousands column. 4 thousands plus 2 thousands plus 1 thousand is 7 thousands.

Abstract



Once children are secure in concrete and pictorial methods, they move onto the formal written method.



As with previous methods, children's place value knowledge is reinforced through the modelling of this method as demonstrated with the pictorial method. Examples are carefully structured to support conceptual understanding.

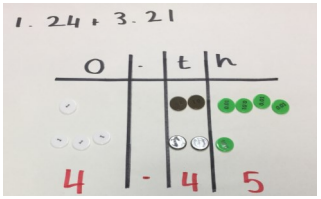
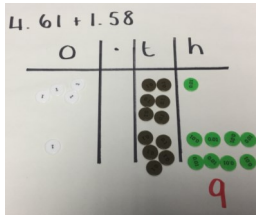
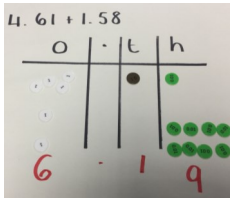
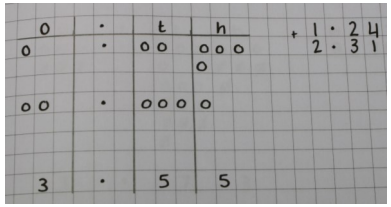
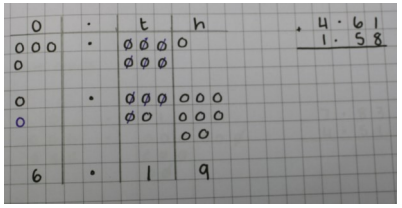
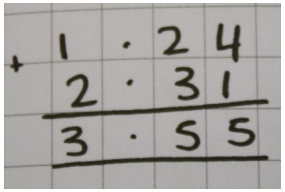
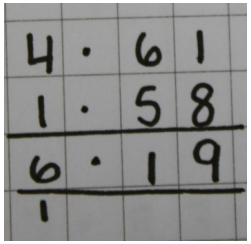
Aspire, Believe, Succeed

Year 4 Calculation

Addition: Add numbers with up to 2 d.p using the formal written method.

In order in begin to add decimal numbers children progress carefully though concrete, pictorial and abstract method.

NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

	Pictorial	Abstract
 Children use place value counters (and/or base ten) to begin to add decimal numbers. Including examples which have different amounts of digits. Examples are carefully structured beginning with questions that do not require exchange. When modelling this method children's place value knowledge is reinforced. Using the example below: 1 hundredth add 8 hundredths is 9 hundredths. 6 tenths add 5 tenths is 11tenths we exchange 10 of these tenths for 1 one into the ones column. 4 ones plus 1 one plus 1 one gives us 6 ones.  	 Children use visual maths to add numbers with up to two decimal places including numbers which have different amounts of digits. They use place holders where necessary. Examples are carefully structured beginning with questions that do not require exchange. When modelling this method, children's place value knowledge is reinforced as demonstrated In the concrete method. 	 Once children have a secure conceptual understanding of addition of decimals, they move onto a formal written method. As with previous methods, children's place value knowledge is reinforced as demonstrated In the concrete method. 

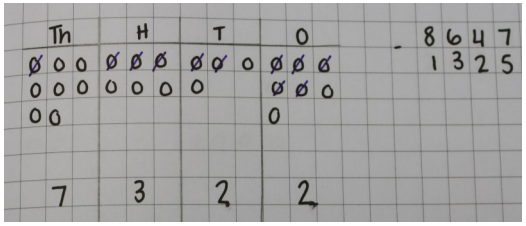
Year 4 Calculation

Subtraction: Subtract number with up to four digits using the formal written method.

In Year 4, children build upon calculation skills developed in Year 3. Prior to the methods taught below, concrete methods (as modelled in Year 3 subtraction) are used to support conceptual understanding.

NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

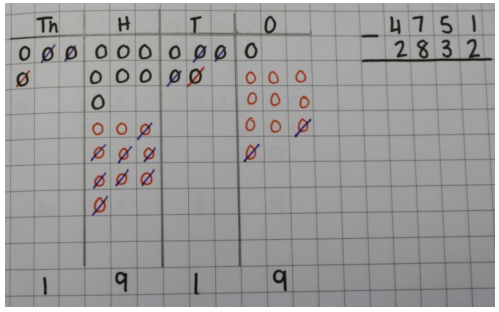
Pictorial



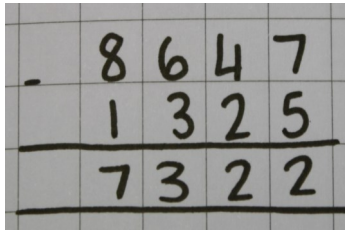
Children use a pictorial method to aid conceptual understanding of subtraction of whole numbers up to four digits. This includes subtracting numbers with different amounts of digits.

Examples are carefully structured to begin with those that do not require exchange.

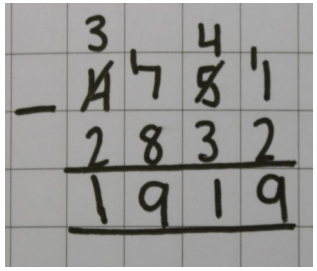
When modelling this method, children's place value knowledge is reinforced. Looking at the second example. We can not do 1 one subtract 2 ones and therefore we exchange 1 ten from the tens column. 11 ones subtract 2 ones is 9. The 4 remaining tens subtract 3 tens gives 1 ten. 7 hundreds subtract 8 hundreds we can not do so exchange 1 thousand for 10 hundreds. 17 hundreds subtract 8 hundreds gives 9 hundreds. The 3 remaining thousands subtract 2 thousands leaves 1 thousand.



Abstract



Once children have a secure conceptual understanding of subtracting whole numbers, they move onto the formal written method.



As with previous methods, children's place value knowledge is reinforced through the modelling of this method. With examples carefully structured to support conceptual understanding.

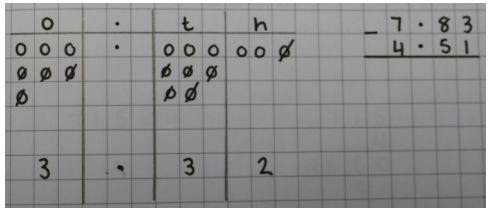
Year 4 Calculation

Subtraction: Subtract numbers with up to 2 d.p using the formal written method of subtraction

In order in begin to subtract decimal numbers children progress carefully though concrete, pictorial and abstract method.

NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

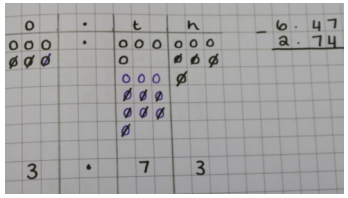
Pictorial



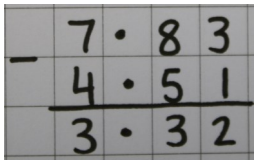
Children use visual maths to subtract numbers with up to two decimal places including numbers which have different amounts of digits. They use place holders where necessary.

Examples are carefully structured beginning with questions that do not require exchange.

When modelling this method, children's place value knowledge is reinforced. E.g. 3 hundredths take away 1 hundredth .

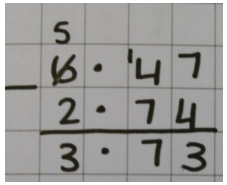


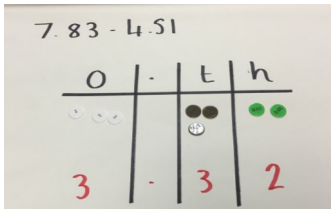
Abstract



Once children have a secure conceptual understanding of subtraction of decimals, they move onto a formal written method.

As with previous methods, children's place value knowledge is reinforced though the modelling of this method.



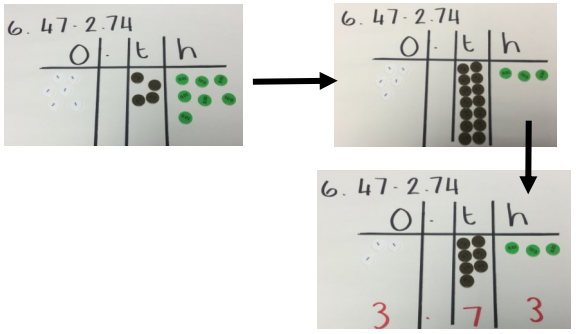


Children use place value counters (and/or base ten) to begin subtracting decimal numbers. Including examples which have different amounts of digits.

Examples are carefully structured beginning with questions that do not require exchange.

When modelling this method children's place value knowledge is reinforced. Using the example below:

7 hundredths minus 4 hundredths is 3 hundredths. We can not do 4 tenths subtract 7 tenths and therefore we exchange 1 one for 10 tenths which allows us to subtract 7 tenths. We can then subtract 2 ones from the 5 remaining units leaving 3 ones.



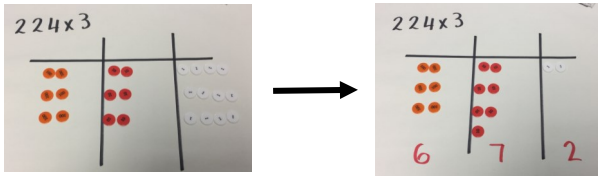
Year 4 Calculation

Multiplication: Multiply a two-digit and a three-digit number by a one-digit number.

In Year 4, children move on and secure methods taught in Year 3 moving on to multiplying a three-digit number by a one-digit number.

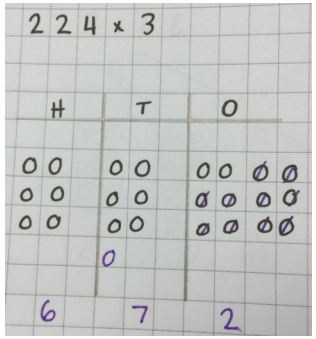
NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

Concrete



Prior to this method, multiplication may be modelled using base ten equipment to begin initial conceptual understanding. Place value counters are then used . In the example above, 3 groups of 224 have been drawn. It is recognised that there are more than 10 ones and therefore 10 ones are regrouped to make 1 ten in the tens column. Examples are structured carefully beginning with those that do not require regrouping.

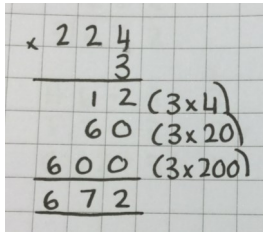
Pictorial

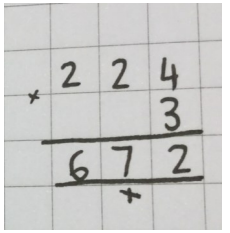


Children then move onto a pictorial representation . In the example above, 3 groups of 224 have been drawn. Children then use their addition skills to find the total.

Examples are structured carefully beginning with those that do not require regrouping.

Abstract





Children then move onto a formal written method.

They begin with an expanded method moving into the short method of multiplication.

Examples are structures carefully beginning with those that do not require regrouping.

Year 4 Calculation

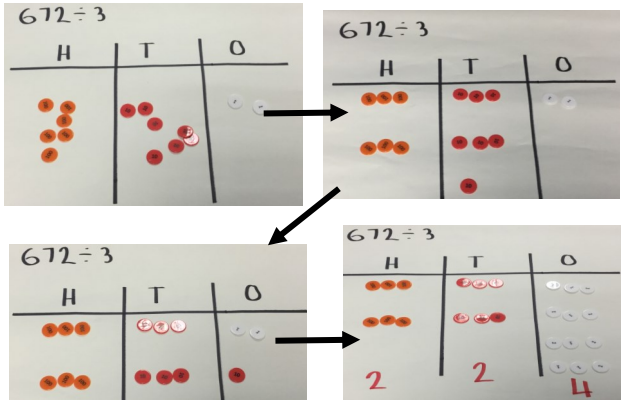
Division: Divide a three-digit number by a one-digit number.

Progressing from Year 3, Year 4 bridge the gap between dividing a two-digit number by a one digit number and dividing a four-digit number by a one digit number.

It is important that children progress carefully between concrete, pictorial and abstract methods.

NOTE: As part of calculation, children are taught to estimate the answer to a calculation and use the inverse to check answers.

Concrete

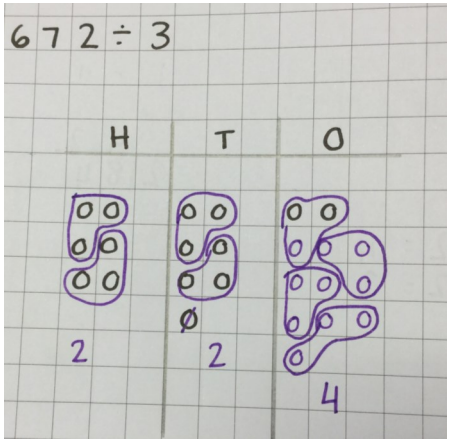


Prior to this method, division may be modelled using base ten equipment. Place value counters are used to represent the three-digit number.

Beginning in the hundreds column, the required amount of groups are then made (see example above). Starting in the hundreds column groups of 3 are made. When making groups of 3 in the tens column there is 1 ten left over which is exchanged into the ones column. The 12 ones are then made into groups of 3.

Examples are structured carefully beginning with those that do not have remainders.

Pictorial

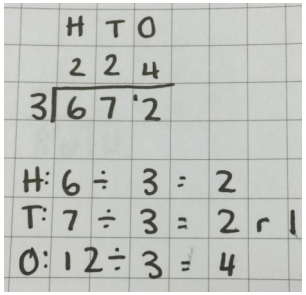


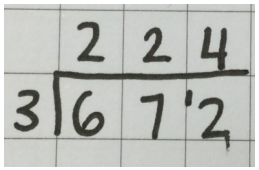
Once secure in the concrete method, children move onto a pictorial method by drawing the three-digit number that they are dividing.

Beginning the in the hundreds column , the required amount of groups are then made (see example above).

Examples are structured carefully beginning with those that do not have remainders.

Abstract





Finally, children move onto the formal written method first beginning with informal jottings.

The same place value conversations are modelled as in the previous methods.

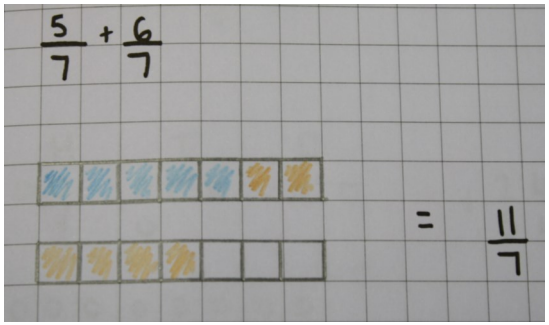
Examples are structured carefully beginning with those that do not have remainders.

Year 4 Calculation

Fractions: Add and subtract fractions with the same denominator.

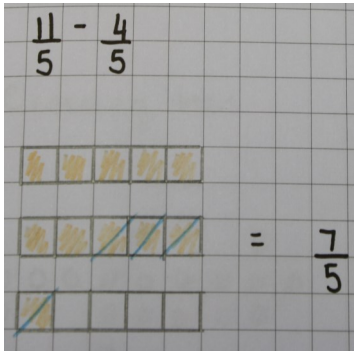
In year 4, children progress into adding and subtracting fractions with the same denominator which go above a whole.

Pictorial



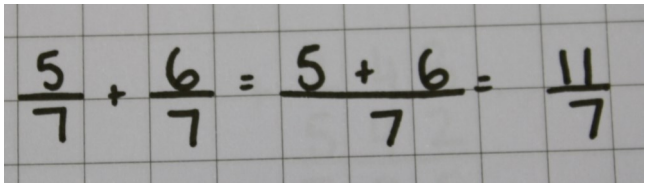
Children begin adding and subtracting fractions with the same denominator using fraction bars.

As seen in the first example children draw 5/7s. They then shade in 6 more—they will recognise that in order to do this they would have to draw another fraction bar. Once the bar is drawn children can find a total.



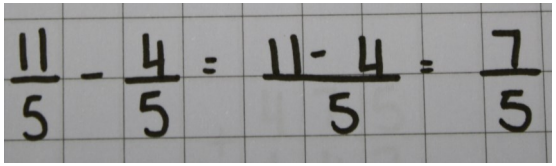
When subtracting ,children begin by shading the correct amount. They then cross out the required number and count the remainder.

Abstract



Once secure, children move onto using a more abstract method.

Children recognise that when adding and subtracting fractions with the same denominator the denominator stays the same (as the sizes of the pieces are the same) we can then add or subtract the numerators.



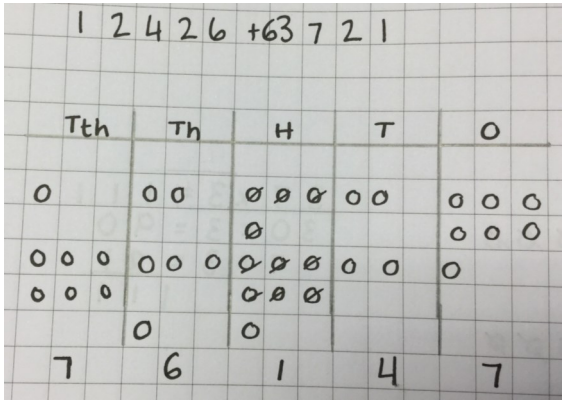
Year 5 Calculation

Addition: Add whole numbers with more than 4 digits using the formal written method of addition.

Children develop their understanding of formal addition based on methods taught in previous years. Concrete methods (as modelled in Year 3 addition) are used to develop conceptual understanding before moving onto the pictorial and abstract methods used below.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

Pictorial

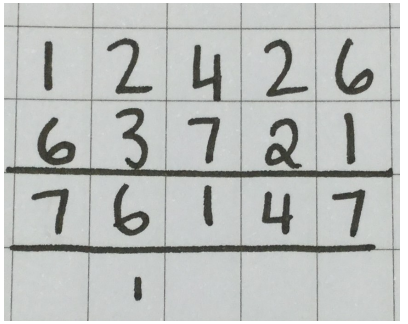


Children use a pictorial method to aid conceptual understanding of addition of whole numbers with more than four digits.

Examples are carefully structured to begin with those that do not require regrouping.

When modelling this method, children's place value knowledge is reinforced. E.g. 6 ones plus 1 one is 7 ones. 2 tens plus 2 tens is 4 tens.

Abstract



Once children have a secure conceptual understanding of addition of whole numbers, they move onto the formal written method.

As with previous methods, children's place value knowledge is reinforced through the modelling of this method.

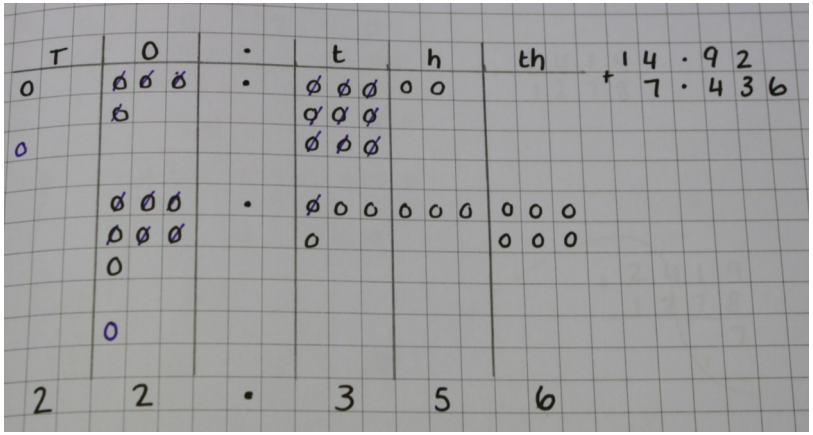
Year 5 Calculation

Addition: Add decimals with up to 3 d.p using the formal written method.

In Year 5, children continue to building up addition of decimals taught in Year 4. Concrete methods (as modelled in Year 3 addition) are used to develop conceptual understanding before moving on to the methods taught below.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

Pictorial

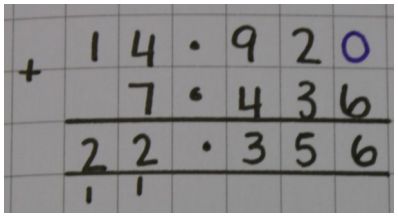


Children use visual maths to add numbers with up to three decimal places. They use place holders where necessary.

Examples are carefully structured beginning with questions that do not require regrouping

When modelling this method, children's place value knowledge is reinforced. E.g. 0 thousandths plus 6 thousandths is 6 thousandths, 2 hundredths plus 3 hundredths is 5 hundredths, 9 tenths plus 4 tenths is 13 tenths. This is one unit and 3 tenths—we carry one unit over to the units column and so on

Abstract



Once children have a secure conceptual understanding of addition of decimals, they move onto a formal written method.

As with previous methods, children's place value knowledge is reinforced though the modelling of this method.

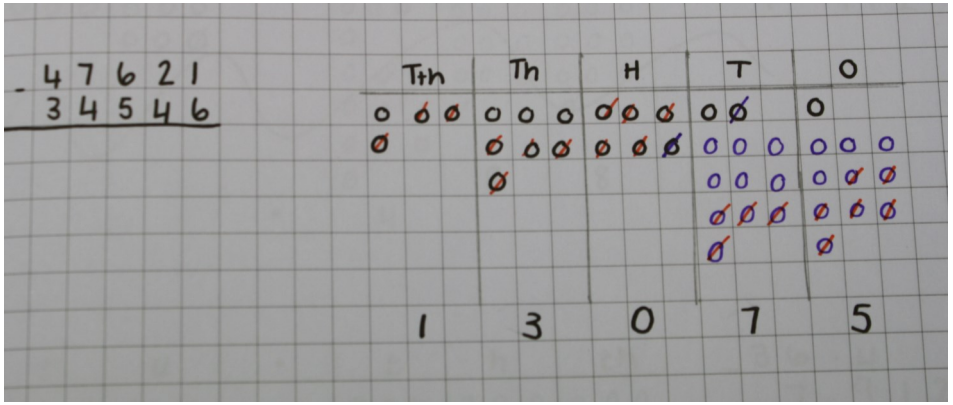
Year 5 Calculation

Subtraction: Subtract numbers with more than four digits using the formal written method of subtraction.

Children develop their understanding of formal subtraction based on method taught in previous years. Concrete methods (as modelled in Year 3 subtraction) are used to develop conceptual understanding before moving onto the methods modelled below.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

Pictorial

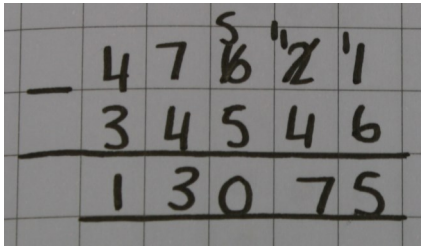


Children use a pictorial method to aid conceptual understanding of subtraction of whole numbers with more than four digits.

Examples are carefully structured to begin with those that do not require exchange.

When modelling this method, children's place value knowledge is reinforced. E.g. one unit take away 6 units, we can not do this and therefore we need to exchange from the tens column.

Abstract



Once children have a secure conceptual understanding of subtracting whole numbers, they move onto the formal written method.

As with previous methods, children's place value knowledge is reinforced through the modelling of this method.

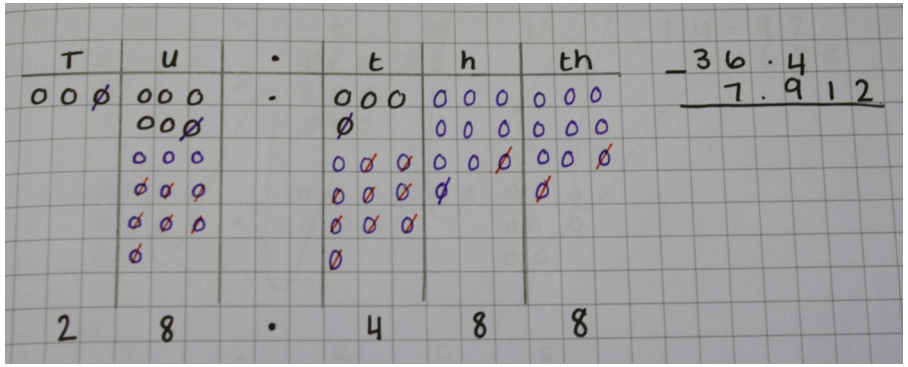
Year 5 Calculation

Subtraction: Subtract numbers with 3 d.p using the formal written method of subtraction.

In Year 5, children continue to building up subtraction of decimals taught in Year 4. Concrete methods (as modelled in Year 3 subtraction) are used to develop conceptual understanding before moving onto the methods taught below.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

Pictorial

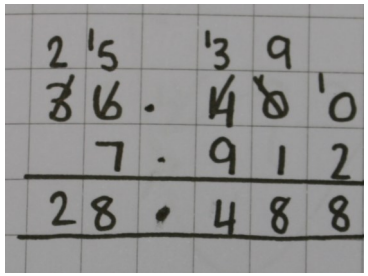


Children use visual maths to subtract numbers with up to three decimal places. They use place holders where necessary.

Examples are carefully structured beginning with questions that do not require exchange.

When modelling this method, children's place value knowledge is reinforced. E.g. 0 thousandths take away 2 thousandths.

Abstract



Once children have a secure conceptual understanding of subtraction of decimals, they move onto a formal written method.

As with previous methods, children's place value knowledge is reinforced though the modelling of this method.

Year 5 Calculation

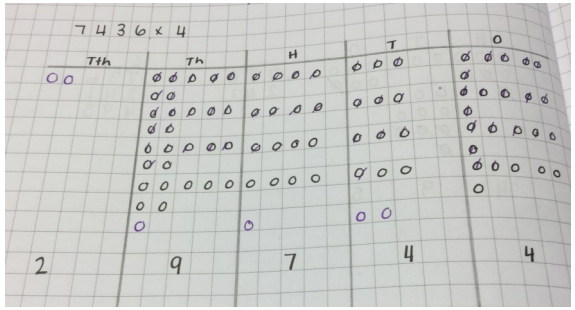
Multiplication: Multiply a four dig-it number by a one digit number using the formal written method of multiplication.

It is important when multiplying by a one-digit number that children are secure in their place value knowledge and can apply this to the method.

If necessary, and to support conceptual understanding, refer to the concrete methods modelled for multiplying by a one-digit number in Year 4.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

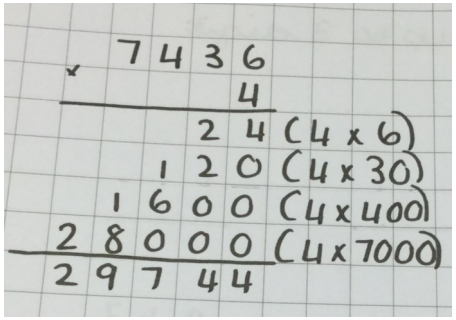
Pictorial



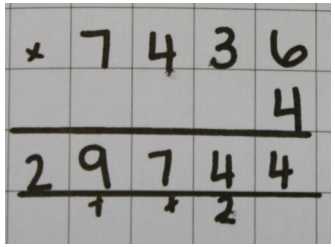
Children extend upon their understanding of multiplying by a one-digit number taught in previous years.

In this example, four groups of 7436 have been drawn. Children then use their addition skills to find the total.

Abstract



Children move onto a less formal abstract method to help bridge the gap between a pictorial method and the formal written method.



Children move onto a formal written version of this however the same place value based conversations are still had when discussing and modelling.

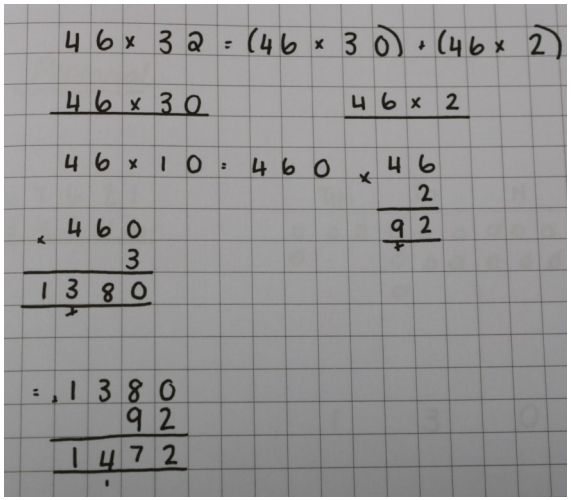
Year 5 Calculation

Multiplication: Use long multiplication to multiply two two-digit numbers.

In year 5, children are first introduced to multiplying by a two-digit number. Children base their understanding on a secure place value understanding of multiplying by a one-digit number.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

Abstract



Children begin to understand multiplying by a 2-digit number as 2 calculations which are merged. They are multiplying by the number of ones, multiplying by the number of tens and the adding these values together.

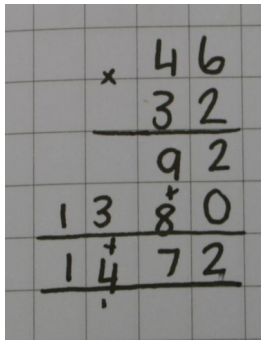
This can be seen in the example above.

46 is multiplied by 30 (by multiplying by 3 and then multiplying by 10)

46 is then multiplied by 2.

These values are then added together.

Careful attention is made to the effect of multiplying by ten and why each time a whole number is multiplied by 10 there is a 0 in the ones column.



Children move onto the formal written method by understanding that they first multiply their 2-digit number by the number of ones.

Following their discussions from the previous method, a 0 is placed in the units column before continuing multiplying by the tens.

These two calculations are then added together to reach the final answer.

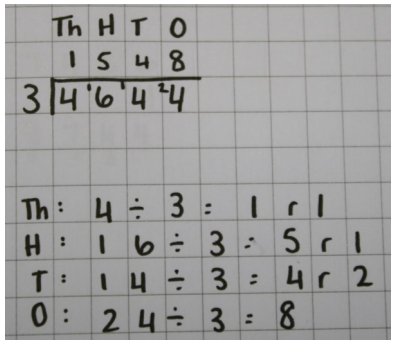
Year 5 Calculation

Division: Divide numbers with up to four digits by a one digit number and interpret remainders.

It is important that children are secure with their place value understanding of this method. Prior to modelling the formal method an abstract/ pictorial method should be demonstrated (see Year 4 division)

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

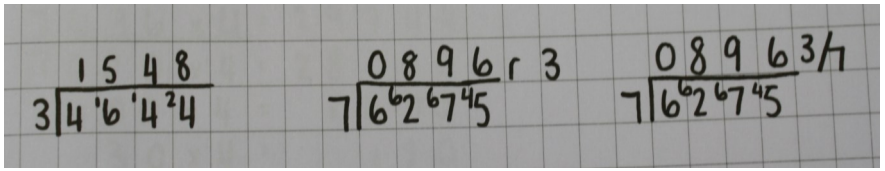
Abstract



Once children are secure with their conceptual understanding of this method a less formal abstract method is introduced and modelled alongside.

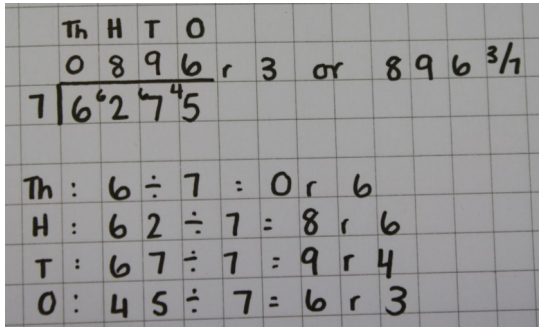
As shown in the two examples, informal jottings are used for each process of the calculation.

Children move into writing remainders and remainders as fractions. In this case there were 3 remainders our of a group of 7.



Finally, children move on to a formal written method with out the use of jottings.

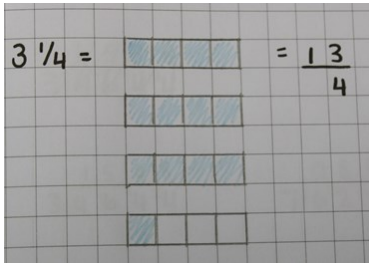
They can effectively discuss and explain the method with their use of place value knowledge.



Year 5 Calculation

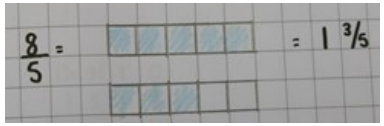
Fractions: Convert between mixed numbers and improper fractions.

Pictorial



Fraction bars are first used to develop conceptual understanding.

3 and 1/4 represents 3 whole bars and 1/4 of a bar which is altogether 13/4/

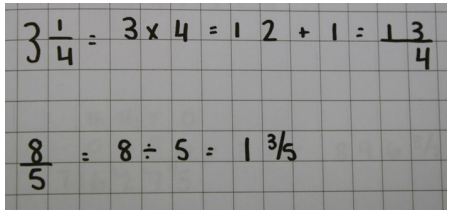


When converting improper fractions to mixed numbers, children recognise that it is an improper fraction and therefore larger than one.

They begin drawing fifths and shading eight in. One whole bar is shaded and 3/5 of another bar is shaded.

Abstract

Once conceptual understanding is developed, children move on to a more abstract approach. They understand that the whole number represents the whole number of bars that are shaded. Using the improper fraction they know how many equal pieces each bar is split into and therefore how many equal pieces are shaded in put the improper fraction.



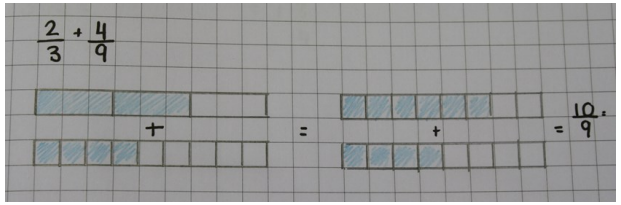
When converting from improper to mixed numbers. Children know they are trying to find how many whole bars are shaded in and what is left over. In the example above, they are trying to make groups of 5. One whole group of 5 can be made from 8/5 and 3 left over which equals 1 whole and 3/5s.

Year 5 Calculation

Fractions: Add and subtract fractions with denominators which are multiples.

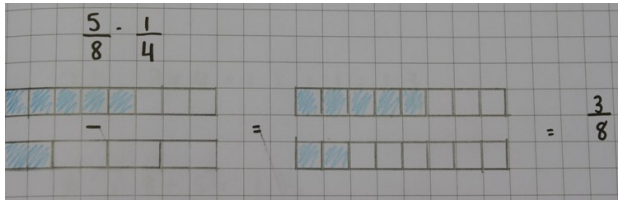
Prior to this, children need to be secure in their addition and subtraction of fractions with the same denominator and why it is important that the denominator is the same before adding or subtracting.

Pictorial

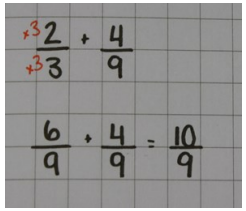


Children recognise that in the two examples that are shown the calculation can not be completed yet because the denominators are not the same and therefore they are adding different sized pieces. Using fraction bars, they recognise that the fraction with the smallest denominator can be written as an equivalent fraction with the same denominator.

Children draw fraction bars to represent and understand this process.



Abstract

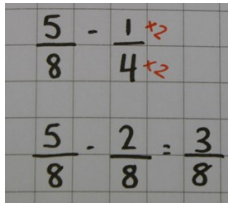


Children recognise that in the two examples that are shown the calculation can not be completed yet because the denominators are not the same and therefore they are adding different sized pieces.

Looking at the fraction with the smallest denominator, using their multiplication knowledge, they see that they can multiply this fraction so that the denominator is the same as the same.

Remembering that whatever is done to the denominator is also done to the numerator both are multiplied so that now both fractions have the same denominator. This can be seen in orange on the examples.

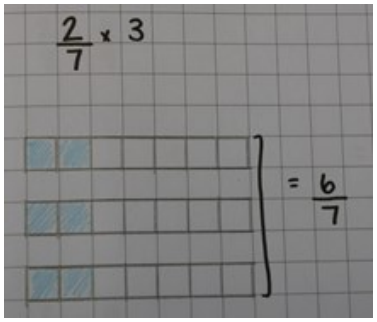
Once the denominators are the same, children can multiply.



Year 5 Calculation

Fractions: **Multiply proper fractions and mixed numbers by a whole number.**

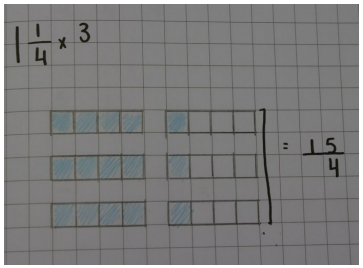
Pictorial



Children begin to understand multiplying proper and mixed number fractions by first using fraction bars.

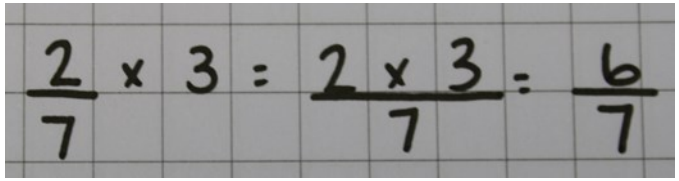
In the first example, 3 bars are drawn each representing 2/7.

There are 6/7 shaded altogether.



In the second example, mixed numbers are investigated. Three bars are drawn to represent 1 1/4. There are 15/5 shaded in altogether.

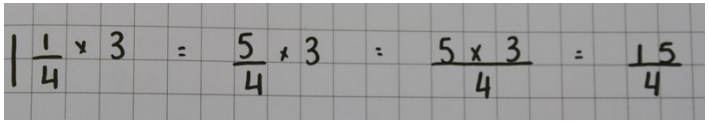
Abstract



When children conceptually understand this process , they move on to a move abstract method.

They understand that the size of the pieces never changes and therefore the denominator doesn't change. The number of equal pieces increases by the value they are multiplying by. Therefore, the numerator is multiplied.

When multiplying mixed numbers, this is first converted to an improper fraction and then the same method is applied.



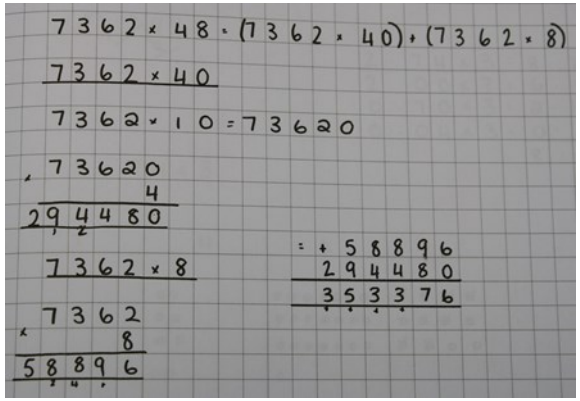
Year 6 Calculation

Multiplication: Multiply numbers up to four digits by a two-digit number using long multiplication.

In Year 6, children base their conceptual understanding on previous years. This can be reinforced prior to beginning teaching.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

Abstract



Children begin to understand multiplying by a 2-digit number as 2 calculations which are merged. There are multiplying by the number of ones, multiplying by the number of tens and the adding these values together.

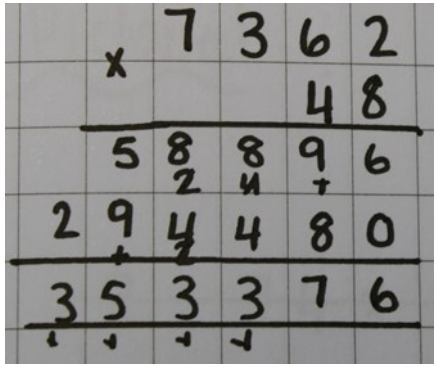
This can be seen in the example above.

7362 is multiplied by 40 (by multiplying by 10 and then multiplying by 4)

7362 is multiplied by 8.

These values are then added together.

Careful attention is made to the effect of multiplying by ten and why each time a whole number is multiplied by 10 there is a 0 in the ones column.



Children move onto the formal written method by understanding that they first multiply their 4-digit number by the number of ones.

Following their discussions from the previous method, a 0 is placed in the units column before continuing multiplying by the tens.

These two calculations are then added together to reach the final answer.

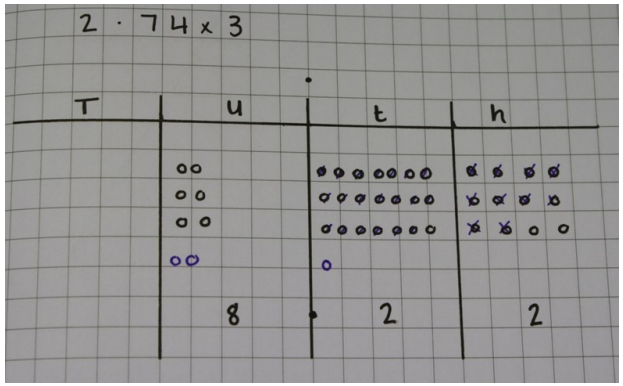
Year 6 Calculation

Multiplication: Multiply a one-digit number with 2 d.p by a one-digit number.

It is important when introducing multiplying decimals that children are secure in their place value knowledge and can apply this to the method.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

Pictorial

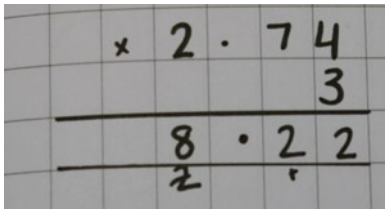


When introducing multiplying a decimal number by a one-digit number, a pictorial method is first introduced.

In this example 3 groups of 2.74 have been drawn in. It is then established that there are 12 hundredths which make 1 tenth and 2 hundredths and therefore 1 tenth is carried over.

There are now 22 tenths which make 2 ones and 2 tenths and so 2 tenths are carried over. This gives 8.22 as an answer.

Abstract



Children move onto a formal written version of this however the same place value based conversations are still have. E.g. 3 lots of 4 hundredths equals 12 hundredths—place 2 in the hundredths column and carry the 1 tenth over and so on.

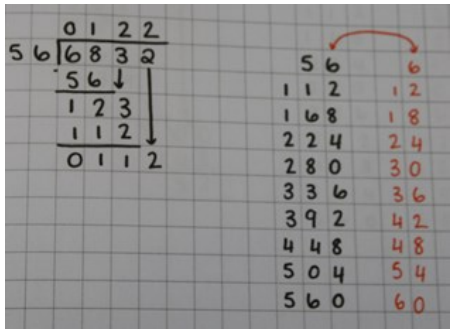
Year 6 Calculation

Division: Divide numbers up to four-digits by a two-digit number using long division writing remainders as whole numbers, fractions or rounding.

When teaching division in Year 6, time is spent to discuss the method used. Children understand the place value implications of the method being taught. For example, we are not doing 6 divided by 56. We are finding how many thousand groups of 56 we can get from 6000. It is important children understand this before moving onto the more abstract example which is demonstrated below.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

Abstract



As a pre-curser to teaching long division children are taught a range of methods to find the first ten multiples of a two-digit number.

Children look at the relationship between how the first ten multiples in the ones column end the same as the first ten multiples of the two-digit number.

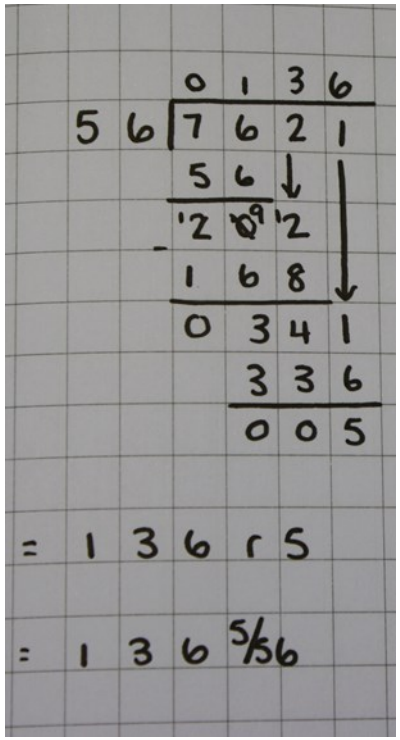
Children are encouraged as much as possible to find these first ten multiples mentally. However, where this is not possible informal jottings are used.

When dividing by a two digit number, children first look in the thousands column. How many groups of 56 can you get out of 6? The answer is 0 so 0 groups are written at the top.

Children then move along—how many groups of 56 can I get out of 68?The answer is 1 so 1 group is written and the top and then taken away underneath leaving 12.

Children can not take any groups of 56 from 12 and therefore the 3 from the tens column is bought down. How many groups of 56 can we get from 123? The answer is 2. Two groups are written at the top and then taken away underneath leaving 11.

We can not get any groups of 56 from 11 so we bring down the 2. How many groups of 56 can we get from 112? The answer is 2. We 2 groups at the top and take away underneath leaving no remainders.



Using the long division taught children then interpret the remainder to fit the context that they have.

When interpreting the remainder as a fraction, children look at how many are left out of the group they were trying to make.

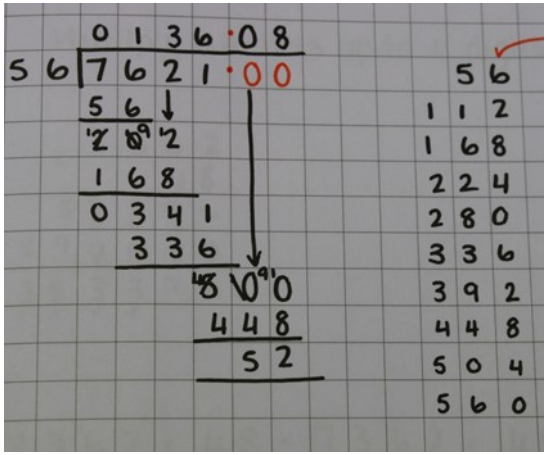
In this example there were 5 left out of a group of 56.

Year 6 Calculation

Division: Use written division in cases where the answer has up to decimal places.

NOTE: As part of calculation, children are taught to estimate and use rounding to check answers to calculations and determine, in the context of a problem levels of accuracy.

Abstract



Children begin writing the first ten multiples. Although children are encouraged to do this as mentally as possible jottings can be used to support this.

Children then follow the same division rules as previously demonstrated.

In order to write the remainder as a decimal children place a decimal point as a 0 as a place holder in the tenths column.

This 0 can be then bought down to form part of the calculation—no groups of 56 can be taken away from 50 so another 0 is placed as a place holder in the hundredths column. This 0 can then be bought down.

Eight groups of 56 can be taken from 500. Groups are written at the top and taken away at the bottom.

Children complete this process up to two decimal places.

Year 6 Calculation

Fractions: Add and subtract fractions (including mixed numbers) with different denominators.

When adding and subtracting fractions pictorial methods from previous year may be used to support conceptual understanding.

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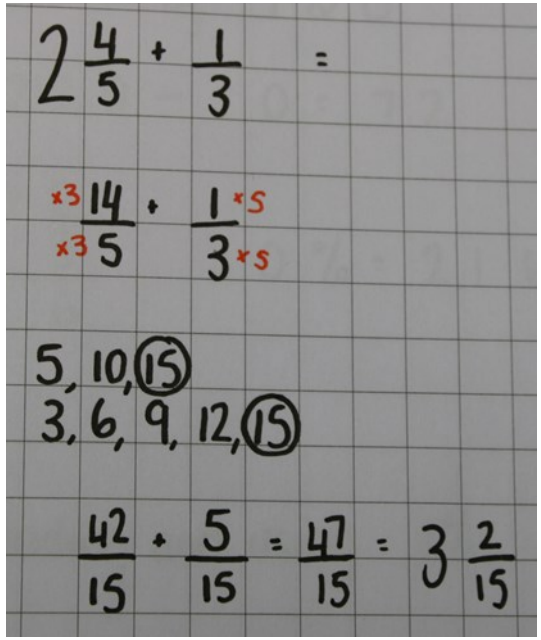


When calculating with mixed numbers, these are converted into improper fractions first.

Children will recognise that they can not add the fractions straight away as the denominators are not the same nor are the denominators multiples of each other.

Children find the lowest common multiple. If confident, children do not need to write this step to find the lowest common multiple.

Using this children convert so that the denominators are the same and then use this to add.

Children will recognise that they can not subtract the fractions straight away as the denominators are not the same nor are the denominators multiples of each other.

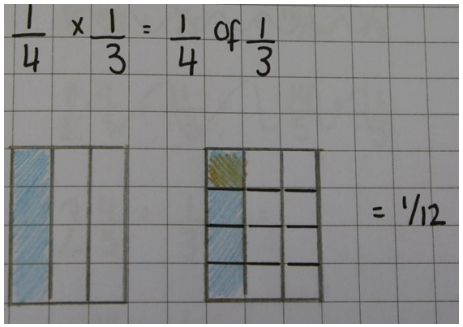
Children find the lowest common multiple. If confident, children do not need to write this step to find the lowest common multiple.

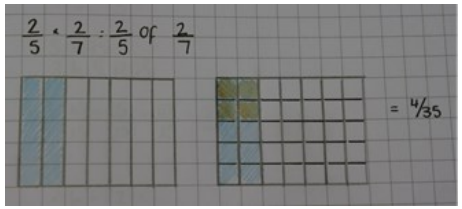
Using this children convert so that the denominators are the same and then use this to subtract.

Year 6 Calculation

Fractions: Multiply pairs of proper fractions.

Pictorial





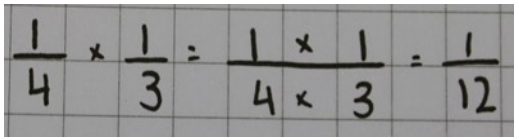
Children understand the multiplication as finding a fraction of another fraction. As seen in the example 1/4 of 1/3.

Children begin drawing a fraction bar of their starting fraction. In this case 1/3, as they are finding 1/4 **of** 1/3.

They then share each third in quarters and shade in 1 as they want 1/4. Resulting in 1/12.

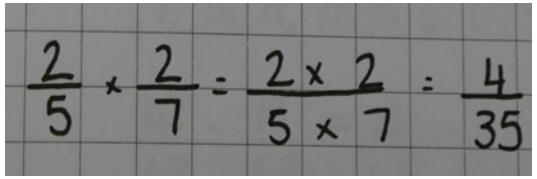
This example is extended below were children are now finding 2/5 of each of the 2/7 that they have shaded.

Abstract



Children move on to an abstract approach.

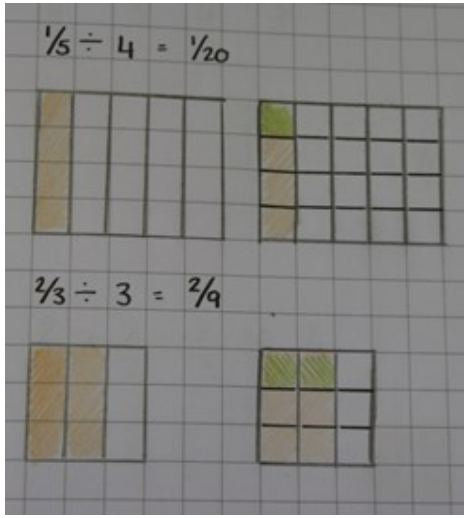
Using the understanding gained from the pictorial method, children multiply to the numerators and denominators to answer the multiplication.



Year 6 Calculation

Fractions: Divide proper fractions by a whole number.

Pictorial



Children use fraction bars to represent division of fractions. They draw the fraction they are starting with as shown in orange.

They then split each equal piece into the divisor. We would receive one of each of the new pieces .

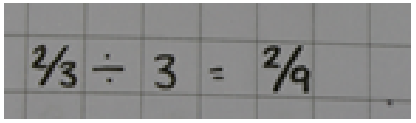
In the first example we would receive 1 out of now 20 equal pieces.

In the second example, we would receive 1 piece from each of the thirds we started with. This would give us 2 out of now 9 equal pieces.

Abstract

Children move on to not using a pictorial method and understand that when dividing the numerator stays the same as we will still receive the same number of equal pieces.

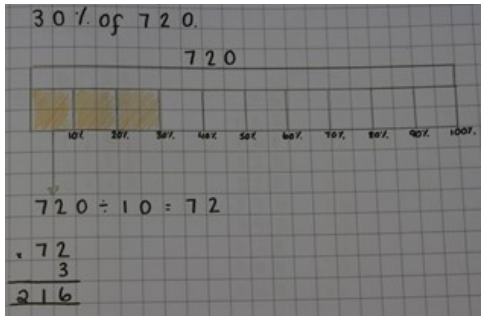
We multiply the denominator as the size of those pieces gets smaller.



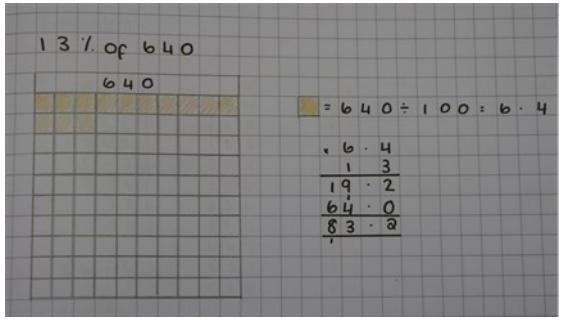
Year 6 Calculation

Percentages: Solve problems involving the calculation of percentages.

Pictorial



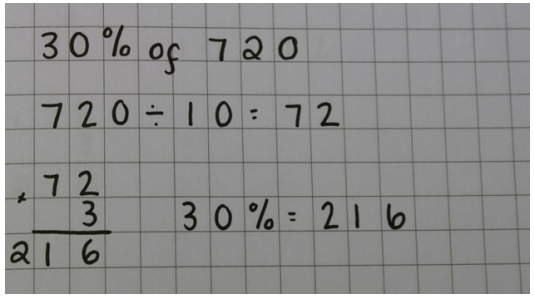
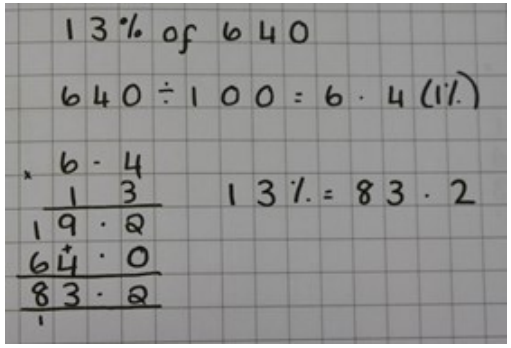
Children begin by using a bar to understand that there is 100% in a whole. Using this they find 10% and use this to find percentages of other multiples of ten.



When finding and using 1% children begin to understand this by using a hundreds square. With each square representing 1%.

Children begin by finding 1% and then move onto using 1% to find other percentages.

Abstract



Children move on to not using the percentage bar or the percentage square as a representation.